

CIS400 (Compiler Construction) Kris Micinski, Fall 2021

## Output of assignment 2

```
; e ::= (let ([x e] ...) e)
     I (lambda (x ...) e)
     l (lambda x e)
     l (apply e e)
; | (e e ...)
; | (prim op e ...)
     l (apply-prim op e)
     l (if e e e)
   | (set! x e)
     | (call/cc e)
     l (quote dat)
```

# Implicit nesting structure, lots of necessary continuations...

```
::= (let ([x e] ...) e)
  l (lambda (x ...) e)
  l (lambda x e)
   (apply e e)
    Te e ...)
   (prim op e ...)
   (apply-prim op e)
  (if e e e)
  | (set! x e)
  | (call/cc e)
  l (quote dat)
```

If we build an interpreter for this *direct-style* language, we end up having to push stack frames at many different forms...

```
(if e e e);; to evaluate first e
(e e ...)
  ;; step through each e until we have
  ;; (v0 v1 ...) where v0 is a closure
(call/cc e);; to eval e to a closure
```

## Why ANF convert?

ANF conversion can be thought of as *explicating* subcomputations

If you've ever "single stepped" in a debugger, executing each subcomputation one at a time...

$$x = 2 + 3 * (4 + 5);$$

True assembly languages **require** every operation be atomic

Because atomic values can fit into registers

```
movq $r0, 4
movq $r1, 5
addq $r0, $r1
movq $r1, 3
mulq $r0, $r1
movq $r1, 2
addq $r0, $r1
```

## Data Layout and Primitive Operations...

Note: primitive calls may (as above) be compiled to instructions (div/sub/...) rather than using an explicit call instruction (e.g., to a function implementing subtraction). However, this depends on data representation: if language is using "boxed" objects, direct uses of, e.g., sub may be impossible because

0xffac130faace0010

of pointer representation...

```
%rax

0xffac130faace0010

Our class: register holds pointer to actual integer value on heap (allows BigInts)
```

0x10

The heap

In this example, we end up pushing lots of stack frames to compute the argument to the call/cc!

```
(define (return-in x e)
  (if (= x 0) e (return-in (- x 1) e)))
(call/cc (return-in 1000 (lambda (x) 3)))
```

For lots of reasons, it will be simpler if there is as little ambiguity as possible in control structure for our language

ANF makes evaluation order explicit in that all forms evaluate either (a) atomically or...

(b) by calling (and getting a return from) a function

## A-Normal Form (ANF) — Definition

In ANF (Administrative Normal Form), all subexpressions (of every expression) are "administratively" bound

ANF allows only **one** form to extend the stack: **let**All values are implicitly return points

## ANF—why do we care (as compiler authors)?

ANF is essentially straight-line code interspersed with function calls, but there is always a definite next step that is either a "call and continue" (let) or "return"

For example, because **i f**'s guard may be evaluated immediately, the evaluation of if will be atomic

This is useful because it mirrors **machine instructions**, assuming the machine has a **call** instruction

```
(let ([x0 (+ 4 5)]
  (let ([x1 (+ 3 x0)])
    (let ([x2 (+ 2 x1)])
      x2)
      ;; imaginary assembly-ish code
    r0 = call(+,4,5)
    r1 = call(+,3,r0)
    r2 = call(+,2,r1)
    ret r2
```

```
;; imaginary assembly-ish code
r0 = call(+,4,5)
r1 = call(+,3,r0)
r2 = call(+,2,r1)
ret r2
```

This intermediate representation is useful to think about as humans, because we often like to think about **blocks of** variables and we are used to think about direct-style call/return

ANF forces us to linearize subcomputations into straight-line sequences, mirroring the block-based nature of assembly

```
(+ 1 (if (f 2) 3 4))
(let ((g391612 (f 2)))
(let ((g391613 (if g391612 3 4)))
(+ 1 g391613)))
```

We let-bind (f 2) (so if's guard is atomic), 3 and 4 are return points, and the top-level if is let-bound to r0

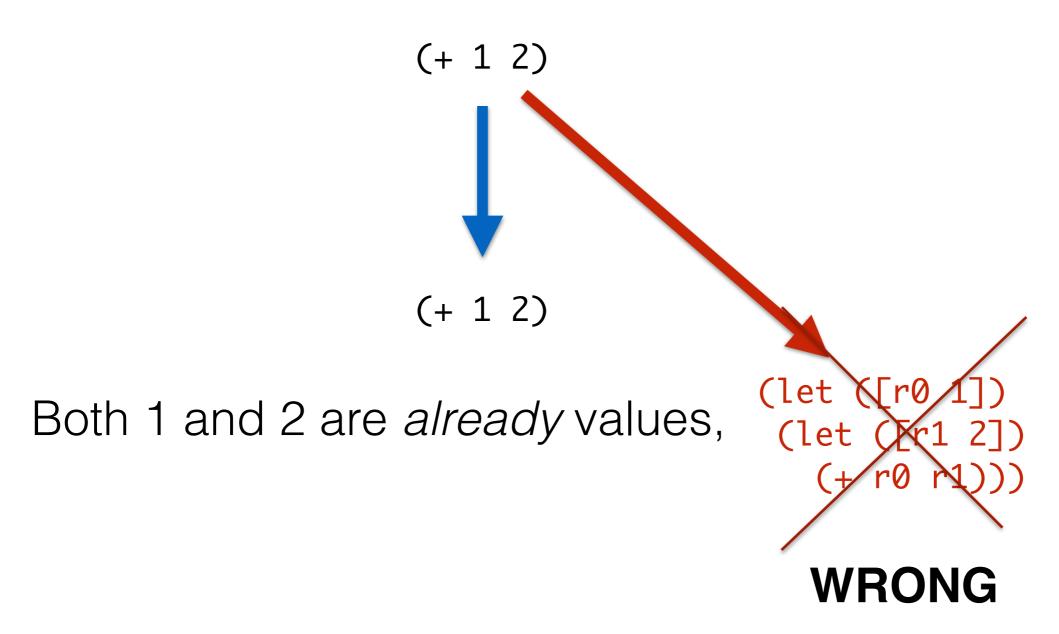
In essence, ANF corresponds to an assembly-like language where we can perform function calls and bind names, but control structure ("where to go next") is always very simple and explicit

Also... Converting our code to ANF will make it significantly easier to perform CPS conversion (next), as continuation structure becomes much simpler in ANF!

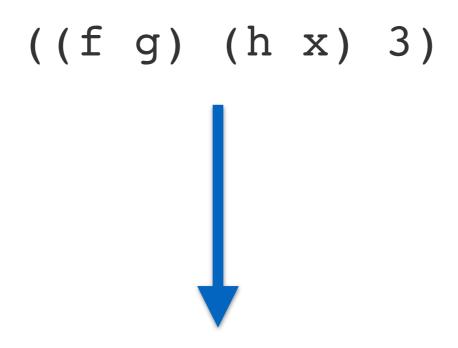
# Values

- Recall: values are atomic objects of the language.
- Syntactically, values are forms which need no evaluation:
  - Variables, constants, quoted datums, etc...
  - · Not applications (e.g., (list 1 2 3)), if, etc...
  - ' '(1 2 3) <-- value</pre>

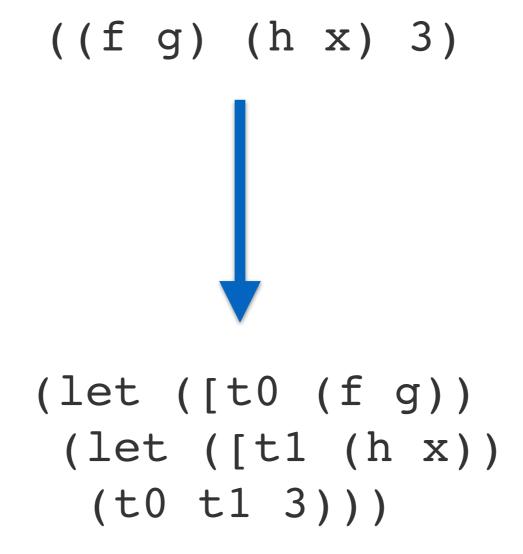




(Don't need to let-bind 1, it's already a value)



Note: 3 already atomic, no binder necessary.



Note: 3 already atomic, no binder necessary.

```
(define (f n)
     (if (= n 0)
          (* n (f (- n 1))))
(f 20)
             (define f
                           Notice how guard is let-bound
              (λ (n)
               \sim (let ((g1478 (= n 0)))
                    (if g1478
                      (let ((g1479 (- n 1)))
                         (let ((g1480 (f g1479)))
                           (* n g1480)))))))
             (f 20)
```

```
(+ (begin (displayIn "hello") 1)
  (begin (displayIn "world") 2))
```



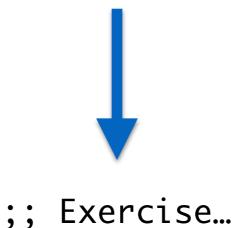
Note that we needed to be careful to ensure ordering

```
(+ (begin (displayIn "hello") 1)
  (begin (displayIn "world") 2))
```

```
(let ([r0 (begin (let ([r1 (displayIn "hello")]) 1))])
(let ([r2 (begin (let ([r3 (displayIn "world")]) 2))])
(+ r0 r2)))
```

Note that we needed to be careful to ensure ordering

```
(+ (begin (displayIn "hello") (displayIn "there") 1)
  (begin (displayIn "world") 2))
```



Note that we needed to be careful to ensure ordering

```
(if (z (+ 2 (call/cc (f y)))) 3 (g z))
(let ([r0
       (let ([r1
              (let ([r2 (let ([r3 (f y)]) (call/cc r3))])
                (+ 2 r2))])
         (z r1))])
  (if r0
      (let ([r4 (g z)])
        r4)))
```

## ANF conversion algorithm — Intuition

- ANF algorithm uses a few key insights:
  - Converts direct-style terms to ANF terms
- Key idea: walk over the term, whenever you encounter a complex expression, if its arguments are not atoms, generate an administrative let-binding for them and then use them as if they were atoms
- Remember, we don't create let bindings for values—those are implicitly return points

Notice how in this term, we get to an **if** term, and the guard isn't atomic, so we *make* it atomic by assigning it an intermediate value...

```
(if (z
                                               ) 3 (g z))
(let ([r0
                 ])
  (if r0
            ))
```

We need to do the same thing with the call to g in the else branch of the let...

```
(if (z
                                              ) 3 (g z))
(let ([r0
                 ])
  (if r0
      (let ([r4 (g z)])
        r4)))
```

Now, we can look at z, we see it's a call to + on 2 and call/cc...

```
(if (z (+ 2 (call/cc (f y)))) 3 (g z))
```

## ANF Conversion Algorithm

## From "The Essence of Compiling with Continuations"

#### The Essence of Compiling with Continuations

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#### Abstract

In order to simplify the compilation process, many compilers for higher-order languages use the continuationpassing style (CPS) transformation in a first phase to generate an intermediate representation of the source the  $\beta$ -value rule is an operational semantics for the source language, that the conventional full  $\lambda$ -calculus is a semantics for the intermediate language, and, most importantly, that the  $\lambda$ -calculus proves more equations between CPS terms than the  $\lambda_v$ -calculus does between corresponding terms of the source language. Translated

#### Four functions:

- (normalize-term e) normalizes a term e to ANF
- (normalize e k) normalizes e to ANF and applies
   k
- (normalize-name e k) converts e to ANF and—if
  the result is complex (i.e., not atomic) calls k on a
  temporary variable which is let-bound to the result
  (making it atomic rather than complex)
- (normalize-name\* es k) ^^ same with multiple es

normalize-term will ANF-normalize the term and return its result...

```
(define (normalize-term e)
  (normalize e (λ (e+) e+)))
```

Note how normalize-term passes a continuation callback to normalize to continue the work...

normalize-name will ANF-normalize e to a value, take its result e+, and then check to see if e+ is a value:

- If it is, then directly apply k
  - This allows us to avoid unnecessary let-binding
- If e+ is **not** a value, it is a complex expression that must be let-bound because k is assuming it is an atomic expression, so let-bind it as a new var x and pass that var to k

Note how normalize-name passes a continuation callback to normalize to continue the work...

For example...

```
(normalize-name (+ 1 2) (lambda (x) x))
;; (let ([x (+ 1 2)]) x)
```

In sum, **normalize-name** will take an expression e, call normalize (which we will see soon) to convert it to ANF, and —if it's not a value—let-bind it to make it a value and then return that value to the callback k.

```
;; convert e to ANF and apply k to result
(define (normalize e k)
  (match e
    ;; lambdas just return themselves to k
    [(\lambda, params, body)
      (k \ (λ ,params ,(normalize-term body)))]
    ;; return any other value to k
    [(? value?)
                             (k e) ))
    ;; to normalize let, first normalize its binder, then
    ;; (by passing a callback) let-bind its result to be used
    ;; in the normalized body
    [`(let ([,x ,eb]) ,e-body)
      (normalize eb (\lambda (e-r)
       `(let ([,x ,e-r])
         ,(normalize e-body k))))
    ;; to normalize an if, normalize e0 to an atomic value t
    ;; and branch on its result
    (if ,e0 ,e1 ,e2)
      (normalize-name e0 (\lambda (e-r)
       (k `(if ,e-r ,(normalize-term el)
                     ,(normalize-term e2)))))]
    ;; to normalize a call...
    [ (,Fn . ,M*)
      (normalize-name Fn (\lambda (t)
       (normalize-name* M* (\lambda (t*)
        (k (,t ,t*)))))
```

```
#lang racket
;; anormalize: A simple A-Normalizer for a subset of Scheme
;; Original Author Matt Might (rewritten by Kris Micinski)
;; http://matt.might.net/
                                                        ;; Expression normalization:
                                                        (define (normalize-term exp) (normalize exp (\lambda (x) x))
(define (atomic? exp)
                                                        ;; normalize
  (match exp
                                                        (define (normalize exp k)
    [`(quote , )
                         #t]
                                                          (match exp
    [(? number?)
                         #t]
                                                            [`(\lambda ,params ,body)]
    [(? boolean?)
                         #t]
                                                              (k (\lambda , params , (normalize-term body)))
    [(? string?)
                         #t]
    [(? char?)
                         #t]
    [(? symbol?)
                                                            [`(let () ,exp)
                         #t]
                                                              (normalize exp k)]
    [(or '+ '- '* '/ '=) #t]
    [else
                         #f]))
                                                            [`(let ([,x ,exp1] . ,clause) ,exp2)
                                                              (normalize expl (\lambda (aexpl)
 (define (normalize-name exp k)
                                                              `(let ([,x ,aexp1])
                                                                 ,(normalize `(let (,@clause) ,exp2) k))))]
   (normalize exp (\lambda (aexp)
      (if (atomic? aexp) (k aexp)
                                                            [`(if ,exp1 ,exp2 ,exp3)
           (let ([t (gensym)])
                                                              (normalize-name expl (\lambda (t)
            `(let ([,t ,aexp]) ,(k t))))))
                                                               (k `(if ,t ,(normalize-term exp2)
                                                                          ,(normalize-term exp3)))))
 (define (normalize-name* exp* k)
                                                            [`(set! ,v ,exp)
   (if (null? exp*)
                                                              (normalize-name exp (\lambda (t)
        (k '())
                                                               `(let ([,(gensym 'x) (set! ,v ,t)])
        (normalize-name (car exp*) (\lambda (t)
                                                                  ,(k '(void))))]
         (normalize-name* (cdr exp*) (\lambda (t*)
                                                            (',f . ,e*)
           (k `(,t . ,t*)))))))
                                                              (normalize-name f (\lambda (t)
                                                               (normalize-name* e* (\lambda (t*)
 ;; Tests:
                                                                (k `(,t . ,t*)))))]
 (pretty-print
                                                            [(? atomic?)
  (normalize-term
                                                             (k exp)]))
   '((f q) (h 3) #f)))
```

## Examples...

```
(pretty-print
 (normalize-term
  '(λ (z)
     (\lambda (x)
       (set! z (f x))))))
(pretty-print
 (normalize-term
  '(+ (if (f x) 0 1) 2)))
(pretty-print
 (normalize-term
  '(let ((id (\lambda (x) x)))
     (let ((apply (\lambda (f x) (f x))))
       ((id apply) (id 3))))))
(pretty-print
 (normalize-term
  '(let ([id (\lambda (x) x)]
          [apply (\lambda (f x) (f x))])
     ((id apply) (id 3)))))
```