Anonymous Author(s)

ABSTRACT

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Datalog allows intuitive declarative specification of logical inference tasks while enjoying efficient implementation via state-ofthe-art engines such as LogicBlox and Soufflé. These engines enable high-performance implementation of complex logical tasks including graph mining, program analysis, and business analytics. However, all efficient modern Datalog solvers make use of shared memory, and present inherent challenges scalability.

In this paper we leverage recent insights in parallel relational algebra and present a methodology for constructing data-parallel deductive databases. Our approach leverages recent developments in parallelizing relational algebra to create an efficient data-parallel semantics for Datalog. Based on our methodology, we have implemented the first MPI-based data-parallel Datalog solver. Our experiments demonstrate comparable performance and improved single-node scalability versus Soufflé, a state-of-art solver.

1 INTRODUCTION

Database systems are broadly declarative, typically supporting expressive query languages. Systems for *deductive databases* such as Datalog further allow persistent rules that specify relations defined intensionally, only in terms of other relations. Picture a database listing inventory and sales for an online business where a set of simple declarative rules are used to update an out-of-stock table or a table listing the total profit earned for each customer. In such systems, expressive reasoning can be embedded alongside ones data and used to generate sophisticated analytics on-the-fly as changes are made.

Effective declarative programming represents a long-standing dream of computing—exchanging code describing *how* to compute for code simply describing *what* to compute. Instead of requiring programmers to themselves balance the concerns of correctness, maintainability, and scalability in each task, declarative programming languages permit users to focus on the first two concerns, writing high-level, correct specifications of *what* should be computed, while allowing the underlying implementation (i.e., *how* the operational mechanics of the program work) to be extracted automatically. This puts significant pressure on the implementation strategy used for declarative languages as it must compete with hand-optimized implementations while remaining generic and effective for a wide variety of applications.

At the same time, this approach presents an opportunity: as effective means are found for parallelizing the semantics of declarative languages, the strategy will apply immediately to all analytics using these platforms. This is already the case for bottom-up (forward chaining) logic programs written in *Datalog*, and related languages with semantics that implement first-order or higher-order

Horn-clause satisfiability. Such programs may be implemented using high-performance relational algebra, as is done in the state-ofthe-art logic-programming language Soufflé [31]. Standard operations on relations such as selection, projection, join, and union may be used in combination to implement efficient kernels that infer new facts from available facts in a (fixed-point) loop. Fortunately, the underlying primitives used in these kernels are inherently quite data-parallel. For example, the Cartesian product of two relations, $R \times S$ may be computed by partitioning the left-hand relation R for a set of threads and then performing a local product $R_i \times S$ for each partition *i*, of *R*, in a trivially parallel manner. Unfortunately, many important inference problems must be scaled beyond single-node parallelism; e.g., state-of-the-art program analyses for Java that are implemented in Soufflé can take many hours and only terminate for lower-precision tunings, targeting real-world codebases [35].

While this approach to parallelizing bottom-up logic programming is already being used to great effect on single-node systems [3], scaling the approach to many-thread clusters using MPI's interprocess communication paradigms has proven a significant challenge. Recent work has introduced techniques for managing parallel relational algebra using MPI on clusters. This has been quite tricky as both communication and decomposition of the computational workload over many nodes must be done explicitly in a dynamically balanced manner, while on shared-memory systems both these problems become nearly trivial when using efficient thread-safe data-structures—tools produced through decades of successful research.

In this paper, we present a synthesis of two ongoing threads of research: (1) an approach to compiling Datalog-like languages to relational algebra for synthesizing fast program analyzers [18], and (2) a scheme for balanced parallel relational algebra using MPI that addresses communication challenges of putting operations on relations in a loop [25]. Putting these ideas together, we are able to present a highly data-parallel deductive database engine that shows promising scaling on the DOE supercomputer Theta.

To the literature, we contribute:

- (1) An approach to developing scalable, data-parallel Datalog solvers using parallel relational algebra. We formalize our approach as a parallel relational algebra machine (PRAM) for which we have implemented a compiler.
- (2) An evaluation of kCFA, a core program analysis algorithm, showing higher performance and scalabiliy compared with Soufflé. In general, we observed varying but comparable performance and improved relative scaling in our comparison studies.

2 BACKGROUND

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Our approach synthesizes two foundational threads: compilation of Datalog-like inference languages to relational algebra kernels

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and recent success enabling the development of data-parallel relational algebra implementations. In this section, we present a summary of these developments to ground our own contributions.

2.1 Relational Algebra

Relations are sets of flat tuples of homogenous arity. By flat, we mean that each tuple consists of base values, for example a 64-bit integer or tagged pointer into a string table. Standard set operations including union, intersection, and product naturally lift to relations.

Projection of a relation *R* restricts it to a particular set of dimensions $\alpha_0, \ldots, \alpha_j$, where $\alpha_0 < \ldots < \alpha_j$, and is written $\prod_{\alpha_0, \ldots, \alpha_j}(R) \triangleq \{(r_{\alpha_0}, \ldots, r_{\alpha_j}) \mid (r_0, \ldots, r_k) \in R\}$. Renaming (i.e., recording) columns can be defined in several ways. We define a renaming operator, $\rho_{\alpha_i/\alpha_j}(R)$, to swap two columns, α_i and α_j where $\alpha_i < \alpha_j$ —an operation that can be repeated to rename/reorder as many columns as desired.

Two relations can also be *joined* into one on a subset of columns they have in common. Join combines two relations into one, where a subset of columns are required to have matching values, and generalizes both intersection and Cartesian product operations.

To formalize natural join as an operation on such a relation, we parameterize it by the number of prefix values that must match, assumed to be the first *j* of each relation (if they are not, a renaming operation must come first). The join of relations *R* and *S* on the first *j* columns is written as $R \bowtie_j S$ and can be defined:

$$R \bowtie_j S \triangleq \{ (r_0, \dots, r_k, s_j, \dots, s_m) \\ \mid (r_0, \dots, r_k) \in R \land (s_0, \dots, s_m) \in S \land \bigwedge_{i=0}^{j} r_i = s_i \}$$

Naturally a system of relational algebra can support a variety of additional operations or compositions of the above operations (e.g., join followed by project followed by reorder) in theory, and usually does in practice for reasons of efficiency.

2.2 Datalog

Datalog is a bottom-up logic programming language supporting a restricted logic corresponding to first-order HornSAT—the satisfiability problem for conjunctions of Horn clauses [1]. A Horn clause is a disjunction of atoms, all but one of which is negated: $a_0 \lor \neg a_1 \lor \ldots \lor \neg a_j$. Atoms are predicates over universally-quantified variables. By DeMorgan's laws, Horn clauses may be equivalently as $a_0 \lor \neg (a_1 \land \ldots \land a_j)$ or equivalently via implication as $a_0 \leftarrow a_1 \land \ldots \land a_j$.

A Datalog program is a set of (Horn clause) rules $P(x_0, \ldots, x_k) \leftarrow Q(y_0, \ldots, y_j) \land \ldots \land S(z_0, \ldots, z_m)$. It is common to have an "input" database of facts called the *extensional database* (EDB), consisting of an explicitly listed (extensional) set of tuples. Running a Datalog program in terms of some EDB reifies the *intensional database* (IDB), all facts (transitively) derivable via the program's rules. The following example program computes the uncle relation from the relations brother and parent :

Efficient implementation strategies for Datalog would evaluate this program by first compiling to relational algebra primitives. On

shared-memory systems, this would involve ordering the parent relation so it can be efficiently joined with brother, then projecting out the shared p column; this is written $\Pi_{1,2}(\rho_{0/1}(\text{ parent }) \bowtie_1 \text{ brother })$. This reduces optimization of evaluation to efficient implementation of the relational algebra primitives. We call a set of RA primitives used to implement a Datalog program a relational algebra *plan* (RA plan).

While some relations can be computed via a fixed number of RA operations in sequence, others must be computed via a fixed-point of a set of operations. For example, *transitive closure* (TC) of a relation or graph is efficiently implemented via a loop (checking whether a fixed-point has been achieved) over a set of high-performance RA operations. Consider the Datalog rules for computing the ancestor relation:

The first rule represents a base case that says any parent is trivially an ancestor, and the second represents the inductive step of inferring that an ancestor ac for x and a parent a for ac implies an older ancestor a for x.

We can also view parent as an input graph defined as a set of edges, and view TC computation as a graph mining problem. Computing the transitive closure ancestor, of input graph parent, is a simple example of logical inference. From paths of length 0 (an empty graph) and the existence of edges in graph parent, we may trivially deduce the existence of paths of length $0 \dots 1$. From paths of length $0 \dots n$ and the original edges in graph parent, we may infer the existence of paths of length $0 \dots n + 1$. The function F_{parent} below performs a single round of inference, finding paths one edge (parental relationship) longer than any found previously and exposing new inferences to be made for the next iteration of F_{parent} . When the computation reaches a fixed-point, the solution has been found as no further paths may be deduced from the available facts.

$$F_{\text{parent}}$$
 (ancestor) \triangleq parent
 $\cup \Pi_{1,2}(\rho_{0/1}(\text{ ancestor}) \bowtie_1 \text{ parent})$

The first rule says that any direct edge in parent implies a path, in ancestor (taking the role of the left operand of union in F_G), and the second rule says that any path (x, ac) and edge (ac, a) imply a path (x, a) (adding edges for the right operand of union in F_{parent}). Other kinds of graph mining problems, such as computing triangles or k-cliques, can also be naturally implemented as Datalog programs [41]. See Section 4 for several case studies on graph mining and program analysis applications.

Each Datalog rule may be encoded as a monotonic function F, mapping databases to databases conjoined with their immediate consequences, where a fixed-point for F is guaranteed to satisfy the corresponding rule. Once a set of functions $F_0 \dots F_m$ are constructed (one for each rule), naïve Datalog evaluation operates by

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iterating the initially empty IDB and input EDB to a mutual fixedpoint for $F_0 \ldots F_m$. Because the EDB includes a fixed number of atoms, and because Datalog programs cannot generate new atoms, termination is guaranteed.

In practice, most "Datalog" implementations are more expressive than this, and most permit some basic built-in operations (e.g., x!=y), and frequently will allow constructors for inductive data types, such as linked lists. However, while most Datalog implementations are ultimately Turing-complete, they optimize for terminating programs accelerated via fast RA operations.

2.3 Implementation via RA

So far, we have elided important optimization and implementation details in favor of focusing on Datalog's semantics. High-performance Datalog solvers employ specializations of general RA operations that combine sequences of simple operations (join, project, and rename) into one efficient combined operation. We have so far presented the so-called naïve evaluation strategy, recomputing all previously-discovered facts at every iteration. Efficient implementations employ incrementalization, tracking a frontier of freshlydiscovered facts to produce yet-undiscovered facts. For example, when computing transitive closure, another relation α is used which only stores the longest ancestry paths-those discovered in the previous iteration. When computing paths of length *n*, in fixed-point iteration n, only new paths discovered in the previous iteration, paths of length n-1, need to be considered, as shorter paths extended with edges from parent necessarily yield paths which have been discovered already. This optimization is known as semi-naïve evaluation [1].

Using semi-naïve evaluation, each non-static relation (those that may be updated in given iteration, such as ancestor) is effectively partitioned into three relations: ancestor $_{_{full}}$, ancestor $_{_{\Delta}}$, and ancestor $_{new}$. ancestor $_{full}$ stores any facts discovered more than one iteration ago; ancestor $_{\Lambda}$ maintains facts that were newly discovered in the previous iteration, and is joined with parent each iteration to discover new facts; and ancestor holds these newly discovered facts only just learned in the current iteration. At the end of each iteration, ancestor Δ 's tuples are added to ancestor $_{_{full}},$ the pointers are swapped for % full ancestor $_{\Delta}$ and % full ancestor $_{\Delta}$ and ancestor is truncated to prepare for the subsequent iteration.

The state of art evaluating Datalog on a single compute node is perhaps best embodied in the Soufflé engine [18-20, 31]. Soufflé systematically optimizes the RA kernels obtained from an input Datalog program, yielding a program for an abstract Relational Algebra Machine (RAM). Figure 1 shows a portion of the exact C++ code produced by Soufflé (v1.5.1) for the two-rule TC program (indentation and code comments have been added by the authors to improve clarity). To compute $\rho_{0/1}($ ancestor $_{\Lambda}) \bowtie_1$ parent, first the outer relation (the left-hand relation-in this case T_{Δ}) is partitioned so that Soufflé may process each on a separate thread via OpenMP (line 1 in Figure 1). For each partition, a 288 loop iterates over all tuples in the current partition of ancestor $_{\Lambda}$ 289

(line 2) and computes a selection tuple, key, representing all tuples in parent that match the present tuple from ancestor $_{\Lambda}$ in its join-columns (in this case, just the second column value, env0[1]). This selection tuple is then used to produce an iterator selecting only tuples in parent whose column-0 value matches the particular tuple env0's column-1 value. Soufflé thus iterates over each $(x, y) \in$ ancestor $_{\Lambda}$ and creates an iterator that selects all corresponding $(y, z) \in$ parent. Soufflé iterates over all matching tuples in parent (line 5), and then constructs a tuple (x, z), produced by pairing the column-0 value of the tuple from ancestor $_{\Lambda}$, env0[0], with the column-1 value of the tuple from parent , env1[1], which is inserted into ancestor $_{new}$ (line 8) only if it is not already in $ancestor_{full}$ (line 6).

	// Partition ancestor , for a pool of OpenMP threads; iterate over parts			
1	for(auto it = part.begin(); it <part.end();++it){< td=""></part.end();++it){<>			
	<pre>// Iterate over each tuple, env0, of ancestor _ (in each partition)</pre>			
2	try{for(const auto& env0 : *it) {			
	// Construct an iterator selecting tuples in parent that match env0			
3	<pre>const Tuple<ramdomain,2> key({{env0[1],0}});</ramdomain,2></pre>			
4	auto range = rel_1_edge->equalRange_1(key,			
	<pre>READ_OP_CONTEXT(rel_1_edge_op_ctxt));</pre>			
	<pre>// Iterate over matching tuples in parent</pre>			
5	for(const auto& env1 : range) {			
	// Has this output tuple already been discovered (is in ancestor)			
6	if(!(rel_2_path->contains(Tuple <ramdomain,2>({{env0[0],env1[1]}}),</ramdomain,2>			
	<pre>READ_OP_CONTEXT(rel_2_path_op_ctxt)))) {</pre>			
	<pre>// Construct the output tuple and insert it into T_new</pre>			
7	<pre>Tuple<ramdomain,2> tuple({{static_cast<ramdomain>(env0[0]),</ramdomain></ramdomain,2></pre>			
0	<pre>static_cast<ramdomain>(envl[1])}}); rol 4 now noth->incort(tuplo</ramdomain></pre>			
0	PEAD OP CONTEXT(rel 4 new path op ctyt)):			
9	}			
10	}			
11	<pre>}} catch(std::exception &e){SignalHandler::instance()->error(e.what());}</pre>			
12	}			
	Figure 1: The join in TC, as implemented by Soufflé.			

Given this architecture, Soufflé achieves good performance by using fast thread-safe data-structures, template specialized for common use cases, that represent each relation extensionally-explicitly storing each tuple in the relation, organized to be amenable to fast iteration, selection, and insertion. Soufflé includes a concurrent Btree implementation [19] and a concurrent prefix-tree implementation [20] as underlying representations for relations. Soufflé does not support MPI or distributed computation of Datalog programs.

...2.4 Balanced Parallel RA

Implementation of Datalog as performant RA suggests a strategy for extracting massive parallelism if these primitive operations themselves can be made highly data-parallel. Several lines of work have approached the challenge of developing schemes for decomposing large RA operations over many parallel threads. The doublehashing approach, with local hash-based joins and hash-based distribution of relations, is broadly the most commonly used method to distribute join operations over many nodes in a networked cluster computer [12, 13, 38]. Recently, both radix-hash join and mergesort join have been evaluated [7] at up to 4k threads.

Another recent approach proposes algorithms for balanced parallel relational algebra (BPRA) adapting the representation of imbalanced relations, using a two-layered distributed hash-table to partition tuples over a fixed set of buckets, and, within each bucket,

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to a dynamic set of *subbuckets* which may vary across buckets [24]. 349 This represents a decomposition of the relation across processes 350 351 that is keyed both on a set of join columns, and also on all other columns to ensure a balanced mapping of tuples to processes. Each 352 tuple is assigned to a bucket based on a hash of its join-column 353 values, but within each bucket, tuples are hashed on all non-join-354 column values, assigning them to a local subbucket. Each bucket 355 and subbucket pair unquuely assigns that group of tuples to a par-356 357 ticular MPI process. This scheme permits buckets that have more 358 tuples to be split across multiple processes uniformly and for the number of subbuckets to increase as the tuples in that bucket in-359 360 creases. This balancing can be done periodically in both the direction of splitting buckets into more subbuckets, or of consolidating 361 them, as needed. To distribute subbuckets to managing processes, 362 BPRA uses a round-robin mapping scheme that requires a very 363 364 small amount of additional communication, but ensures that no process manages more than one subbucket more than any other. 365 Locally, subbuckets store tuples using B-trees (an approach also 366 367 used by Soufflé, although their data structures have undergone particular engineering refinements). This carries performance advan-368 tages over the double-hashing approach's use of hash tables. Cru-369 370 cially, hash-tables can also lead to complications in a distributed 371 setting where a resizing operation may delay synchronization.

Figure 2 shows a schematic diagram of the BRPA join algorithm 372 in the context of an incrementalized TC computation. A join op-373 374 eration can only be performed for two co-located relations: two relations each keyed on their respective join columns that share a 375 bucket decomposition (but not necessarily a subbucket decomposi-376 377 tion for each bucket). This ensures that the join operation may be performed separately on each bucket as all matching tuples will 378 share a logical bucket; it does not ensure that all pairs of match-379 ing tuples will share the same subbucket as tuples are assigned to 380 subbuckets (within some bucket) based on the values of non-join 381 columns. 382

383 The first step in a join operation is an intra-bucket communica-384 tion phase within each bucket in which every subbucket receives all tuples for the outer relation, across all subbuckets (while the 385 inner relation only needs tuples belonging to the local subbucket). 386 387 After this, a local join operation (corresponding to a Datalog rule, with possible projection and renaming) can be performed in ev-388 ery subbucket in parallel. Output tuples from these local joins may 389 each belong to an arbitrary bucket in the output relation, so an 390 MPI all-to-all communication phase shuffles the output of all joins 391 to their managing processes (preparing them for any subsequent 392 393 rules or iterations). Upon receiving output tuples from the previ-394 ous join, each receiving process inserts them into the local B-tree for each applicable R_{new} . It then propagates R_{Δ} into R_{full} and R_{new} 395 becomes R_{Δ} for the next iteration. If no new tuples have been dis-396 covered, globally, a fixed-point has been reached and iteration may 397 398 halt.

Intra-bucket communication (shown on the left of Figure 2) uses MPI point-to-point communication to shuffle tuples from each subbucket of the outer relation to subbuckets of the inner-relation, which is then able to perform local, per-subbucket joins. It may seem appealing to fuse the final all-to-all communication phase among buckets with the intra-bucket communication of the subsequent iteration, sending new tuples (for R_{Δ} in the next iteration) 407

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directly to all subbuckets of the inner relation; however, doing this fusion forgoes an opportunity for per-subbucket deduplication and yields meaningful slowdowns in practice.

The local join phase proceeds in a parallel and unsynchronized fashion. Each process iterates over its subbuckets, performing a single join operation for each. Our join is implemented as a straightforward tree-based join as shown in the center of Figure 2. In this diagram, colors are used to indicate the hash value of each tuple as determined by its join-column value. Once received, the outer relation's tuples are iterated over, grouped by key values, where, for each, a lookup is performed to select a portion of the inner relation's B-tree where all tuples have a matching key value (in the case of TC computation, this is selecting the first column of parent). For two sets of tuples with matching join-column values, we effectively perform a Cartesian product computation, yielding one tuple for all possible pairs of outer and inner tuple.

Each output tuple has projection and renaming performed onthe-fly; in the case of TC, the prior join columns that matched are projected away. These tuples are locally deduplicated, organized, and staged for transmission to new managing subbuckets in their receiving relation. After evaluating a rule, each output tuple destined for a head-relation R belongs to R_{new} and must be hashed on its join columns; in the case of TC, this is the rightmost column of ancestor. Join columns are hashed to determine the bucket and non-join columns to determine the subbucket; together bucket and subbucket determine a managing process via the current roundrobin mapping (stored on every process). An all-to-all communication phase (shown on the right side of Figure 2) transmits materialized joins to their new bucket-subbucket decomposition in headrelation R_{new} . The managing process for each bucket and subbucket involved is obtained from a local round-robin map and tuples are organized into buffers for MPI's All_to_allv synchronous communication operation. When this is invoked, all tuples are shuffled to their destination processes.

Finally, after the one synchronous communication phase per iteration, each R_{Δ} is locally propagated into R_{full} , which stores all tuples discovered more than 1 iteration ago. New tuples are checked against this R_{full} to ensure they are genuinely new facts, and are inserted into a B-tree for R_{new} on each receiving process to perform remote deduplication. At this point, the iteration ends, R_{new} becomes R_{Δ} for the subsequent iteration, and an empty R_{new} is allocated. If no new tuples were actually discovered in the previous iteration, a fixed-point has been reached and no further iterations are needed as the database as stabilized with respect to all rules of inference.

BPRA is notable for allowing two kinds of load-imbalance to be remediated dynamically across fixed-point iterations. *Spatial load imbalance* occurs when a relation's stored tuples are mapped unevenly to processes due to key-skew or inherent imbalance in relation's distribution of tuples. *Temporal load imbalance* occurs when the number of output tuples produced varies significantly across iterations.

BPRA includes three main algorithms for adjusting the representation of a relation or RA operation to improve both these kinds of balancing. *Bucket refinement* is a dynamic check of each bucket to see if its subbuckets are significantly heavier than average. When



Figure 2: Shows the major phases of a BPRA join in the context of a TC computation.

this is detected, it triggers a refinement in which new subbuckets are allocated to support the larger number of tuples in this specific bucket. Bucket consolidation is the reverse and occurs only if there are a significant number of refined buckets. It consolidates buckets into fewer subbuckets when spatial imbalance has again lessened. Last, iteration roll-over allows particularly busy iterations to be interrupted part-way, with completed work being processed immediately via an added communication phase and with the residual workload from the iteration "rolling over" to a new iteration. This improves robustness in the face of temporal imbalance, preventing crashes at the cost of an additional sychronization phase and poorer deduplication behavior.

PARALLEL RA MACHINE

We develop the standard techniques for compiling Datalog-like languages to RA, and for parallelizing RA over large numbers of threads using BPRA, into a Parallel Relational Algebra Machine (PRAM) and its intermediate representation (IR). Soufflé's RAM is a model for deductive databases in terms of shared-memory relational algebra on a single machine. We introduce PRAM as a evolution of this concept that suits the unique challenges and opportunities of applying BPRA to logical inference tasks.

In the example of Soufflé's compiled C++ in Section 2, any kary join operation could be implemented as a series of k nested for loops (with partitioning among threads, efficient selecting iterators, etc). By contrast, BPRA imposes a key restriction to facilitate data-parallelism: all joined relations must use indices that have precisely homogenous join columns. This means a rule such as

$$H(x,y,z) := B0(w,x,y), B1(y,z), B2(z)$$

must be evaluated using two sequential binary joins, since B0 and B1 share a different column in common than do B1 and B2. While trinary or k-ary joins that are homogenous in their join columns are conceivable via BPRA, they are not common in our Datalog code. The fact that we must use binary joins, and cannot reuse indices for their prefixes [36], represent key restrictions that countervail Soufflé's approach to optimizing Datalog for sharedmemory systems. However, with several key innovations, we manage and exploit the unique distributed setting of our parallel RA operations and obtain an approach that can scale well.

We implement PRAM using BPRA. BPRA's approach to parallel RA is amenable to iterated RA operations over relations with highly dynamic topologies, but it has several challenging limitations we must overcome:

- Lacking of support for heterogenous k-ary joins,
- Inability to run operations in parallel—in BPRA, each operation has its own synchronous all-to-all communication phase.
- Lack of support for tracking multiple indices of relations, adding new tuples to each index.

3.1 PRAM IR

Our definition of a compiled PRAM program or IR is shown in Figure 3. A program is a directed acyclic graph among compiled strongly connected components (SCCs), of program rules, indicating which other SCCs must be run before each SCC can be run. SCCs with no incoming dependencies may be run immediately,

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l	ir \in PRAM = $\mathcal{P}(SCC) \times \mathcal{P}(SCC \times SCC)$
2	$scc \in SCC = \mathcal{P}(Rule)$
, I	rule \in Rule ::= (rule hclause bclause)
5	(rule hclause bclause prim)
5	(rule hclause bclause)
2	(arule hclause bclause)
)	hclause \in HClause ::= (hrel var, ⁺)
)	hrel \in HRel ::= (rel-select name arity index)
1	bclause \in BClause ::= (brel var ⁺)
3	Brel \in BRel ::= (rel-version name arity index ver)
ł	prim \in Prim ::= (op var ⁺)
5	name \in Name = $\langle symbols \rangle$
5	$var \in Var = \langle symbols \rangle$
3	on $\in \Omega$ = (primitive operations)
)	arity \in Arity = \mathbb{N}
)	index \in Index $= \mathbb{N}^*$
l •	$ver \in Vercion = \{delta full\}$
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Figure 3: PRAM domains used to define the core IR we target.

and SCCs that contain only a single non-recursive rule are nonrecursive and are not iterated to a fixed point because a single iteration always guarantees output consistent with the rule. PRAM supports four fundamental kinds of rules: a unary copy rule that propagates one relation into another, with possible reordering and projection; i.e., H(y,x) := B(x,y,z).; a copy with primitive operation that can filter or extend tuples; i.e., H(x,y) := B(x,y), x < y.; a binary join rule that joins two relations with possible reordering and projection; i.e., H(z,x) := B(x,y), B1(y,z).; and finally, an administrative copy rule between a canonical index for a relation and a non-canonical index for a relation.

Our system designates exactly one index for each relation as canonical (this may be the only index for a relation), and creates administrative rules that, acting like a unary copy rule, propagate newly discovered tuples from a canonical index to each of the non-canonical indices. The canonical index is always used in the head of a rule and our compiler generates appropriate indices and administrative copy rules. Note that an hclause is the same as a bclause except that it must be the canonical index and does not need a version tag, as newly discovered tuples are always placed in H_{new} . Body clauses are specific to either the version **delta** or **full**, an artifact of semi-naïve evaluation.

3.2 Implementation

Our implementation of a Datalog compiler and run-time is written in Racket and C++, and is composed of several major passes:

Parsing and lexing. We support typical Datalog notation that overlaps with a substantial fragment of syntactic niceties supported

by Soufflé. We track source locatoins explicitly so we can report errors and we've included support for a few dozen common built-in operators to be attached to rules, such as the comparison x < y.

Organization. A first pass performs simplification and canonicalization steps. For example, we allow suggestions to be given for how to order rules as an extension, these are broken apart into a sequence of rules in this pass. Rules with multiple head clauses can also be split effectively into multiple rules with a single head-clause each. Wildcard variables, as in the clause $r(_,x)$ are re-

named to a unique anonymous variable; e.g., $r(_3,x)$.

Static unification. A second pass performs transitive static unification of variables that are explicitly unified by a built-in comparison, as in p(x,x),q(y),x=y, so equal variables across relations use the same variable name and within the same relation use a built-in to filter that relation; this example is converted to $p(x,_0),q(x),x=_0$.

Partitioning. The next pass partitions complex rules into a set of simple rules that form a linear chain of dependence on one another. For example, the rule

a(x,y,z) := b(w,x), c(x,y), d(y,z).

is compiled into a sequence of two binary rules, inserting an internal relation representing the half-evaluated rule:

> a(x,y,z) :- b(w,x), int(x,y,z). int(x,y,z) :- c(x,y), d(y,z).

As balanced parallel relational joins must be performed on two relations with an identical selection index (to guarantee a compatible parallel decomposition of the two relations), the only rules permitted after this pass are unary copy rules that may reorder or project columns, unary built-in rules that may also perform a generative or filtering built-in operation (such as x < y), or a binary rule that joins two relations, projects some columns, and reorders columns for the head relation.

Complex rules that join four or more relations at once, are likewise partitioned into a linear chain of joins, each performed after the last. We also experimented with creating balanced binary trees of joins, and with various heuristics for partitioning some complex rules roughly in half, before recuring to partition each partition of body clauses. In nearly every case, we observed between $5 \times$ and $25 \times$ the overall tuple-load in these experiments (vs strictly linear chains of rules), representing a very substantial blow-up in intermediate relations. Intuitively, this is because in a linear chain it takes a greater number of iterations to compute the rule, more join operations between starting the rule and adding facts to the head relation, however the tuples involved are always maximally grounded and filtered by all relations taking into account so far. Using balanced binary trees of joins optimizes for lower latency, but leads to constraints apparent in the original rule being taken into account only after a much larger number of intermediate facts are materialized, at significant expense.

As the goal of our system is to exploit the massive data-parallelism of balanced parallel RA operations, we favor pipelining a longer sequence of RA operations in a linear chain, with the exception of

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cases where two subsets of body clauses have completely disjoint sets of variables, as in the example

$$h(x,y) := f(a,x), g(x,b), p(c,y), q(y,d).$$

For this input, our compiler will produce two *independent* binary rules, for f and g and for p and q, followed by a single binary rule to compute the Cartesian product int0(x),int1(y) :

As the Cartesian product is the actual semantics of our original rule, it does not represent a spurious blow-up. Note that the compiler will detect that variables such as a or b are not required for the head, and so can be pruned from intermediate relations as well.

Selection splitting. This pass looks at the binary rules generated in the previous pass and determines the needed set of indices for each relation. This is a set of ordered subsets of their columns that may be used as a key for efficient access in a parallel join operation. If a relation is used in the body of a binary rule, it must have an index for the exact subset of columns it has in common with the other relation used in the binary rule, because we require such compatible matching indices for our parallel join algorithm.

This pass also decides which index is *canonical*, and modifies rules so that the head of every rule is the canonical index for that relation. Administrative rules are then added to propagate discovered tuples to all indices once discovered in the canonical index. These admin rules are essentially unary rules that copy tuples with possible column reordering. This makes it natural to compact the communication needed to maintain a set of indices for a relation with the normal communication used during a parallel join, in pipelined fashion. This is to say, the iteration after a tuple is discovered, it is copied to all its indices during the single communication phase shared by all rules.

Stratification. uses a modified Tarjan's algorithm [37] to compute a directed graph of strongly connected components (SCCs) in the dependency structure of rules. For example, rules that can be run upon initialization only once will appear as rules whose body relations are already available and never modified.

Incrementalization. prepares the program for semi-naïve evaluation by explicitly splitting each relation into three versions, a **new**, **delta**, and **full** version as described previously. The body clauses of rules are modified so that static relations (those that do not change when this rule is evaluated) draw tuples from the **full** version, while dynamic relations must use the **delta** version. When two dynamic relations are joined, these are split into three rules that join **full** with **delta**, **delta** with **full**, and **delta** with **delta**. For complex k-ary join rules, these combinatoins blow up exponentially, so it ends up being convenient we are stuck with having already partitioned these down to chains of binary rules.

C++ *emission*. Finally, the incrementalized rules are written out as a driver in C++ corresponding to PRAM IR code in the previous section. That is to say, our backend's API interfaces to the IR the

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AST described in the last section. There is an object for encoding an administrative rule between two relations with a particular renaming and projection and another for encoding a join rule or a rule that operates on a relation using a built-in primitive to filter or extend the relation as tuples are emitted.

Run-time system. Our backend then finally interprets this PRAM IR, evaluating it efficiently in terms of our extension to the original BPRA source [25]. We have modified the library for BPRA into a more general run-time for PRAM IR. The original library was not developed to allow multiple RA rules to be evaluated in parallel, leading to some engineering challenges in terms of meta-data transfer and keeping track of all relations. We add a logical inference engine object which can be populated with any number of relations and can act generically as a primitive RDBMS and can accept a PRAM IR and set of input relations to evaluate a program and extract the final IDB.

Instead of running each RA operation in an SCC, one at a time, we modify evaluation to interleave all RA operations in a collective single operation with one shared communication phase. Communication is non-uniform, where every process sends different amounts of data to every other process. This is typically implemented using MPI_alltoallv, but, in order to facilitate this nonuniform communication we first have to share the offsets and sizes of all relations and processes, so that every process has a consistent, global view. This meta-data exchange is implemented by MPI_alltoall. After this metadata exchange, we populate send buffers and receive buffers on every process before invoking MPI_alltoallv.

Unlike plain BPRA, every process performs a large batch of local joins (or copies, reorderings, projections, etc) for all given rules in the current SCC. This means that before a single comunication phase, each process will have generated output for potentially a large number of PRAM IR rules. We have introduced an crucial optimization in the form of comm-compaction where we concatenate all-to-all send buffers across all rules into one large buffer that can be transmitted in a single communication epoch. This step significantly cuts down communication costs, especially for compute intensive problem such as kCFA (see section 4) that have several rules in a single SCC and at each step of a collective fixed-point iteration for that SCC. This crucial improvement to RA that would otherwise be individually parallel, but not across multiple operations, requires ordering information to be broadcast during the epoch's fixed meta-data transfer, but appears to grant improved scalability versus Soufflé.

4 CASE STUDIES

In this section, we motivate PRAM by its application to compute transitive closure, k-cliques, and kCFA (a program analysis). To compare our implementation against a known baseline, we benchmark our PRAM-based implementation on a single node against Soufflé, the state-of-the-art Datalog engine. In the next section, we demonstrate the true power of PRAM by scaling these experiments to the Theta supercomputer.

4.1 Graph Mining

Graph-pattern mining (GPM) includes a rich source of core problems that highlight the expressivity of deductive databases. As a first example we consider transitive closure (TC). We can imple ment TC using the following Datalog program, which iteratively
 computes the path relation:

⁸¹⁶ path(x,y) :- edge(x,y). ⁸¹⁷ path(x,z) :- path(x,y) e

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path(x,z) :- path(x,y), edge(y,z).

To compile this Datalog program to PRAM IR, we generate two initial administrative rules to set up path and prepare for the bulk of the work to be done in a subsequent SCC:

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       ; Admin rule to load index for edge on column-1:
822
       (arule
823
        ((rel-select edge 2 (1)) ident a1)
824
        ((rel-version edge 2 (1 2) delta) a1 ident))
825
       ; The first Datalog rule as a binary join rule:
       (rule
826
        ((rel-select path 2 (1 2)) x y)
827
        ((rel-version edge 2 (1 2) total) x y))
828
       ; The next two rules are in an SCC together,
829
            stratified to run after the previous rules.
830
       ; A rule to join path and edge:
831
       (rule
832
        ((rel-select path 2 (1 2)) x z)
833
        ((rel-version path 2 (2) delta) y x)
834
       ((rel-version edge 2 (1) total) y z))
835
       ; Admin rule to propagate discovered paths to
         the index for path on column-2:
836
       ÷
       (arule
837
        ((rel-select path 2 (2)) a1 a0)
838
        ((rel-version path 2 (1 2) delta) a0 a1))
839
       The third rule implements the iterative extension of path to com-
840
       pute TC. Observe that tuples are pulled from the delta version, im-
841
```

plementing semi-naïve evaluation.

Figure 4: The rule for computing 4-cliques from pairs of overlapping 3-cliques combined with a 2-clique. The existence of the top three subgraphs, as represented in the 2cl and 3cl relations, implies the 4-clique below.

Another standard graph mining problem is that of k-clique computation. While it is possible to leverage application-specific insights to calculate cliques (see Section 6 for further discussion), kcliques can naturally be calculated using the intuition in Figure 4— -forming a canonical ordering of nodes and computing k-cliques in increasing order by k. This is represented via the following Datalog program: Anon.

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; Compute undirected 2-cliques in canonical order	871
2cl(x, y) :- graph(x, y), x <y.< td=""><td>872</td></y.<>	872
2cl(x, y) :- graph(y, x), x <y.< td=""><td>873</td></y.<>	873
; compute 3-cliques (order already checked in 2cl)	874
3cl(x, y, z) :- 2cl(x,y), 2cl(y, z), 2cl(x, z).	875
; compute 4-cliques	876
4cl(w, x, y, z) :- 3cl(w, x, y),	
3cl(x, y, z),	877
2cl(w, z).	878
(, -).	879

4.2 Program Analysis

Static program analysis is a key and impactful application of Dataloglike solvers that attempts to develop an accurate bounded model of program behavior based only on the program's source text. Program analyses are constructed using a variety of different theories and approaches; what these approaches share in common is the goal of obtaining sufficient precision for specific program properties while guaranteeing analysis termination, and ideally, efficiency. This central challenge of static analysis is made explicit in the methodology of *abstract interpretation* [14]. An abstract interpretation of a program evaluates its input source code in terms of imprecise or abstract values and machine components, permitting a careful loss of precision in exchange for reasonable bounds on analyis complexity.

A wide variety of abstract interpretations can be systematically engineered as Datalog programs, as has been extensively explored in the literature [18, 21, 22, 29, 42]. In particular the DOOP framework [9] for points-to analysis of Java, originally developed for LogicBlox, has been ported and optimized for Soufflé.

A class of these algorithms known as flow-analyses model the propagation of data-flow information or control-flow information through a target program [26]. Data-flow analysis (DFA) requires control-flow analysis (CFA) to obtain any reasonable precision for functional languages, for multi-paradigm languages like Java that support closures and methods associated with objects, or for structured languages with function pointers, as in C/C++: data-flow properties and control-flow properties are naturally entangled and must be simulated together to obtain a model with any reasonable precision [32, 33]. CFAs form an important foundation for analysis of most programming languages, in particular highly dynamic languages, and are often extended with additional client analyses for tracking relations among variables [5] or for verifying sophisticated contracts using abstract symbolic execution [28]. Systematic approaches to abstract interpretation of abstract-machine-based semantics [40] allow analyses to be developed from a variety of standard (concrete) abstract machines that precisely specify a language's semantics [27].

This systematic development of an abstract abstract machine from a concrete abstract machine yields is highly configurable and tunable, so it corresponds to a broad design space of analyses that strike subtly different trade offs between precision of result and complexity of analysis [17]. One classic instantiation of this framework yields *k*-call-sensitive control flow analysis (*k*CFA), a wellordered hierarchy of CFAs with increasing precision and complexity as parameter *k* is increased. Our implementation of *k*CFA for the plain lambda calculus is about 40 lines in Datalog and can be easily tuned to any *k* to increase its degree of context sensitivity.

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We also wrote a worst-case input generator based on the worstcase input for *k*CFA discussed in [39]. This allows us to scale up either the term size, we call (t) or the context-sensitivity (k). Be-

```
low is a fragment showing how free variables are computed:
932
       // Every variable is free at a reference to it
933
       free(x, e) :- var-ref(e, x)
934
       // At unary application a free variable for either
935
        // subexpression is free at the call-site.
       free(x, e) :-
936
         app(e, e0, e1),
937
         free(x, e0) or free(x, e1).
938
       // At a lambda abstraction, variables free in the
       // body that are not the formal parameter, are free
939
       free(x, e) :-
940
         lambda(e, y, body),
941
         free(x, body),
         x != y.
942
943
```

Free variable computation propagates information up the AST recusively, and forms an SCC in the compiled PRAM IR that is stratified before the primary CFA logic runs.

5 EVALUATION

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In this section we sought to understand the behavior of our system on a single node. To do this, we ran several microbenchmarks comparing single-node performance of Soufflé vs. our MPI-based implementation.

5.1 Dataset and HPC platforms

We perform our experiments on the Theta Supercompter at the Argonne National Lab and on a machine rented via Amazon Web Services (AWS). For AWS, each of our experiments was run on an instance of type m5d.24xlarge consisting of 96 virtual CPUs (Intel Xeon Platinum 8000) and 384 GiB of RAM and NVMe-based SSD storage. Of these 96 virtual CPUs, we ran experiments utilizing up to either 60 processes (for MPI-based imlementation) or threads. Theta supercomputer is a Cray machine with a peak performance of 11.69 petaflops, 281,088 compute cores, 843.264 TiB of DDR4 RAM, 70.272 TiB of MCDRAM and 10 PiB of online disk storage. Theta uses the Dragonfly network topology and is backed by a Lustre filesystem. Theta's node is a Intel KNL 7230 which comprises of 64 physical cores.

5.2 Strong scaling on AWS

To compare the single-node performance of our PRAM-based implementation versus Soufflé, we ran each case study using representative input data. We performed TC using a directed graph of the Arxiv High-Energy Physics paper citation network (consisting of 34,546 nodes and 412,578 edges) compiled by Gehrke et al. [16]. Second, we performed *k*CFA using a scaled-down version of the experiments. We use experiments labled *t-k* with a specific number of terms (*t*) and degree of sensitivity (*k*), as described in section 3.2. For our experiments here, we set term size (*n*) to be 100, and precision (*t*) to be 6.

We compiled each of our experiments using the compiler described in Section 3. We modified our compiler to generate a Soufflé program consisting of only binary joins and benchmark the results. We then used Soufflé's compiled mode to produce an optimized binary to run and minimizing I/O overhead by dumping the smallest output relation. We performed each experiment three



times, reporting the average of each of the runs, though runtime was roughly consistent across runs. For each of our experiments, we validated the correctness of results of Soufflé against our MPIbased implementation by checking both implementations produce the same set of tuples.

The results of our experiments are shown in Figure 5. We plot time (in seconds) along the y axis against process / thread count along the x axis. PRAM achieves better performance than Soufflé for kCFA in our benchmarks. We believe this is because Soufflé parallelizes individual joins, but does not interleave joins to perform them in parallel (further discussion is included in Section 3.2). Because kCFA contains more rules than our other benchmarks, the difference between sequential and parallel joins becomes more apparent. This demonstrates one advantage to our approach even at smaller scales.

For transitive closure computation our experiments showed modestly⁴⁰³³ decreasing runtime for Soufflé, however, we observed poor scaling 1034 characteristic when compared to PRAM. At a high level, our results 1035 demonstrate that our system scales better than Soufflé as degree 1036 of parallelism increases but achieves worse constant factors. One 1037 key difference between PRAM and Soufflé is tuple representation. 1038 While Soufflé employs highly-optimized shared memory datastruc-1039 tures (discussed briefly in Section 2). PRAM uses messsage passing 1040 and an off-the-shelf B-tree implementation to communicate and 1041 1042 represent tuples. Because of this, when lots of tuples are generated during an iteration PRAM will allocate large amounts of memory 1043

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to exchange messages and represent tuples. We see underlying tuple representation as an important but orthogonal issue to our underlying scaling approach, and plan to investigate using Soufflé's datastructures in future work.

5.3 Strong scaling on Theta

Every node on Theta has 64 physical cores. This allowed us to run single-node experiments on the machine till 64 cores. We ran two single node experiments run at 32 and 64 cores. We were unable to run experiments at smaller scale due to memory constraints. We ran a k-CFA worst-case instance with 80 terms and k = 7, which took 2648 iterations to complete, turning 724 EDB facts into 165,389,799 IDB facts. We observe a speed-up of $1.76 \times$ and scaling efficiency of 88% while going from 32 to 64 processes. Our experiments are indicative of healthy scaling.

RELATED WORK 6

To our knowledge, we present the first general-purpose technique for implementing data-parallel deductive databases. However, there are several areas of related work in relational algebra andprogram analysis.

1068 Relational Algebra. Our work directly builds upon that of Ku-1069 mar and Gilray, who implement parallel relational algebra prim-1070 itives and evaluate their scalability on supercomputers [24, 25]. Their implementation leverages the observation that joins can be 1071 1072 distributed to a cluster via a double-hashing approach, consisting 1073 of local hash-based joins and hash-based distribution of relations. 1074 Their double-hashing approach is inspired by the earlier work of 1075 Cheiney et al. [13] and Cacace et al. [12], who describe data-parallel 1076 strategies for computing transitive closure.

Barthels et al. describe a system for distributing the radix hash join and merge-sort join algorithms [7]. Their implementation scales to 4,096 cores via MPI and reaches extremely high tuple throughput at peak load. Work by Kim et al. and Balkesen et al. demonstrates how these joins may be further accelerated via AVX/SIMD instructions [6, 23]. While this work successfully scales a single join iteration, it does not reorganize or balance tuples to allow subsequent joins, and thus does not readily enable the fixed-point computation necessary for deductive databases.

The recent work of Kumar and Gilray enables fixed-point iteration over hash-based joins. Tuples are distributed via a twolayered distributed hash-table which multiplexes tuples onto a statically fixed set of buckets and dynamically-tunable set of subbuckets [24]. Each tuple is assigned a bucket based on the hash of its 1090 join columns; this then enables local hash-based joins. Next, allto-all communication is performed to communicate the result of each join to its appropriate bucket and subbucket. In subsequent work they develop strategies to enable spatial and temporal load balancing of tuples across the cluster, and use these techniques to perform the largest-ever computation of transitive closure [25].

Program Analysis and Datalog. Deductive databases offer an attractive option for the implementation of large-scale program analyses as they enable declarative analysis specification alongside efficient solving via modern Datalog engines. the DOOP framework

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by Smaragdakis et al. poincered an elaborate context-sensitive pointsto analysis for Java implemented in Datalog [10, 35]. DOOP originally used the LogicBlox Datalog engine to achieve an order of magnitude speedup compared to a predecessor hand-written pointsto analysis for Java [4]. DOOP was later ported to the Soufflé Datalog engine, which enabled further scalability via Soufflé's singlenode task-level parallelism [3]. While Soufflé represents the stateof-the-art analysis platform, it is fundamentally limited in that it cannot provide data parallelism, hindering it from operating beyond a single node. By contrast, our parallel relational-algebra approach can likely be scaled to clusters.

There are several other notable efforts in distributed and parallel program analysis that achieve scalability via application-specific task-level parallelism. For example, Aiken et al.'s Saturn program analysis system includes a distributed mode via MPI, which they anecdotally report achieves scalability [2]. Their system distributes the analysis via a worklist of function summaries and distributing work among the cluster. This approach assumes that the analysis is summarization-based and does not offer data parallelism. Similarly, there have been multiple efforts to distribute symbolic execution [11, 30, 34]. Symbolic execution is a program testing technique that executes programs on symbolic inputs, branching to collect a set of *path conditions* in the case of multiple successor states. Symbolic execution is naturally parallelized using a worklist representing a frontier of program states. One limitation of this work is the inherent memory blowup due to the necessary copying of path conditions to implement task-level parallelism. As future work, we plan to study how to integrate SMT solvers such as Z3 [15] into our parallel relational algebra to support symbolic execution, as we expect our system could naturally distribute path conditions through the cluster. The recent Formulog system harmoniously integrates Datalog, functional programming, and constraint solving, and may provide useful inspiration for future work [8]. In contrast to these systems, our approach offers true data parallelism, enabling the entire cluster to make progress on the analysis at once rather than requiring application-specific task deliniation.

7 CONCLUSION

Over the past few years, exciting advances in high-performance Datalog solvers have enabled new frontiers in large-scale static analysis development. However, current-generation Datalog solvers are fundamentally limited to a single machine. In this paper, we presented a methodology building upon emerging work in dataparallel relational algebra that allowed us to build the first dataparallel Datalog solver. Our solver is built on a novel parallel relational algebra machine, PRAM, which makes several key decisions to enable implementing Datalog rules via data-parallel relational algebra. We see this as a foundational step forward in the implementation of high-performance logical inference engines. Our case study benchmarks demonstrate that our PRAM-based approach achieves better single-node scalability than Soufflé, the state-ofthe-art Datalog engine. Additionally, we show promising initial scalability of up to 2,016 nodes on the Theta supercomputer. In future work, we hope to leverage PRAM to build next-generations platforms for graph mining, program analysis, and other largescale logical inference problems.

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